## PHYS 2300 and 2305: General Physics I and II Formulas

## Chapter 1

Trig Formulas

| $\sin \theta=\frac{\text { Opposite }}{\text { Hypotenuse }}$ | $\theta=\sin ^{-1}\left(\frac{\text { Opposite }}{\text { Hypotenuse }}\right)$ |
| :---: | :---: |
| $\cos \theta=\frac{\text { Adjacent }}{\text { Hypotenuse }}$ | $\theta=\cos ^{-1}\left(\frac{\text { Adjacent }}{\text { Hypotenuse }}\right)$ |
| $\tan \theta=\frac{\text { Oppostie }}{\text { Adjacent }}$ | $\theta=\tan ^{-1}\left(\frac{\text { Oppostie }}{\text { Adjacent }}\right)$ |
| $a^{2}=b^{2}+c^{2}$ |  |

Vectors

|  | $\vec{A}+\vec{B}=\vec{C}$ |
| :--- | :---: |
| Where |  |
| Vector Addition by | $\overrightarrow{C_{x}}=\overrightarrow{A_{x}}+\overrightarrow{B_{x}}$ |
| Components | $\overrightarrow{C_{y}}=\overrightarrow{A_{y}}+\overrightarrow{B_{y}}$ |
| Then to find $\vec{C}$ use |  |
| $c^{2}=a^{2}+b^{2}$ |  |

## Chapter 2

Velocity

| Average Velocity | $\bar{v}=\frac{\text { displacement }}{\text { time }}=\frac{\Delta \bar{x}}{\Delta t}$ or $\bar{v}=\frac{\Delta \bar{d}}{\Delta t}$ | 2.2 |
| :--- | :---: | :--- |
| Average Speed | average speed $=\frac{\text { distance }}{\text { time }}$ | 2.1 |
| Instantaneous Velocity | $v=\lim _{\Delta t \rightarrow 0} \frac{\Delta \bar{x}}{\Delta t}$ | 2.3 |

Acceleration

| Average Acceleration | $\bar{a}=\frac{\Delta v}{\Delta t}$ | 2.4 |
| :--- | :---: | :---: |
| Instantaneous <br> Acceleration | $a=\lim _{\Delta t \rightarrow 0} \frac{\Delta \bar{v}}{\Delta t}$ | 2.5 |

Motion of a particle with constant acceleration

| $v=v_{0}+a t$ | 2.4 |
| :--- | :--- |
| $x=\frac{1}{2}\left(v_{0}+v\right) t$ or $d=\frac{1}{2}\left(v_{0}+v\right) t$ | 2.7 |
| $x=v_{0} t+\frac{1}{2} a t^{2} \operatorname{Or} d=v_{0} t+\frac{1}{2} a t^{2}$ | 2.8 |
| $v^{2}=v_{0}^{2}+2 a x$ or $v^{2}=v_{0}^{2}+2 a d$ | 2.9 |

## Chapter 3

## Average Velocity/Acceleration

| Average Velocity | $\bar{v}=\frac{\Delta \bar{x}}{\Delta t}$ or $\bar{v}=\frac{\Delta \bar{d}}{\Delta t}$ | 2.2 |
| :--- | :---: | :---: |
| Average Acceleration | $\bar{a}=\frac{\Delta v}{\Delta t}$ | 2.4 |


| Projectile Motion |  |  |
| :---: | :---: | :---: |
| $X$ direction | $Y$ direction |  |
| $v_{x}=v_{0 x}+a_{x} t$ | $v_{y}=v_{0 y}+a_{y} t$ <br> or $v_{y}=v_{0 y}+g t$ | 3.3 |
| $x=\frac{1}{2}\left(v_{0 x}+v_{x}\right) t$ | $y=\frac{1}{2}\left(v_{0 y}+v_{y}\right) t$ <br> or $d=\frac{1}{2}\left(v_{0 x}+v_{x}\right) t$ | 3.4 |
| $x=v_{0 x} t+\frac{1}{2} a_{x} t^{2}$ | $y=\frac{1}{2}\left(v_{0 y}+v_{y}\right) t$ |  |
| or $d=v_{0 x} t+\frac{1}{2} a_{x} t^{2}$ | $y=1$ <br> or $h=v_{0 y} t+\frac{1}{2} g t^{2}$ | 3.5 |
| $v_{x}^{2}=v_{o x}^{2}+2 a_{x} x$ | $v_{y}^{2}=v_{o y}^{2}+2 a_{y} y$ <br> or $v_{x}^{2}=v_{o x}^{2}+2 a_{x} d$ | 3.6 |

Relative Motion | $\overrightarrow{v_{A C}}=\overrightarrow{v_{A B}}+\overrightarrow{v_{B C}}$ |
| :---: |
| $\overrightarrow{v_{A B}}=-\overrightarrow{v_{B A}}$ |

## Chapter 4

Newton's Second Law

| General | $\Sigma \vec{F}=m \vec{a}$ | 4.1 |
| :--- | :--- | :---: |
| Component form | $\Sigma F_{x}=m a_{x}$ | 4.2 |

## Gravitational Force

| Gravitational Force | $F=G \frac{m_{1} m_{2}}{r^{2}}$ | 4.3 |
| :--- | :---: | :---: |
| Weight | $\mathrm{W}=\mathrm{mg}$ <br> Where $g=G \frac{m_{1}}{r^{2}}$ |  |

G=Universal Gravitational Constant $=6.67 \times 10^{-11} \mathrm{Nm}^{2} / \mathrm{kg}^{2}$
Friction

| Static Friction <br> (maximum) | $f_{s}{ }^{\max }=\mu_{s} F_{N}$ | 4.7 |
| :--- | :---: | :---: |
| Kinetic Frictional | $f_{k}=\mu_{k} F_{N}$ | 4.8 |

Chapter 5

| Speed | $v=\frac{2 \pi r}{T}$ | 5.1 |
| :--- | :---: | :--- |
| Centripetal <br> Acceleration | $a_{c}=\frac{v^{2}}{r}$ | 5.2 |
| Centripetal Force | $F_{c}=\frac{m v^{2}}{r}$ | 5.3 |
| Banked Curve | $\tan \theta=\frac{v^{2}}{r g}$ | 5.4 |
| Satellites in circular | $v=\sqrt{\frac{G M_{E}}{r}}$ | 5.5 |
| orbits | $T=\frac{2 \pi r^{3 / 2}}{\sqrt{G M_{E}}}$ | 5.6 |

NOTE:
$\mathrm{M}_{\mathrm{E}}$ mass of earth $=5.98 \times 10^{24} \mathrm{~kg}$
$r_{E}$ radius of earth $6.38 \times 10^{6} \mathrm{~m}$
$\mathrm{G}=6.67 \times 10^{-11} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{kg}^{2}$


| Work done by constant Force | $\begin{aligned} & \hline W=(F \cos \theta) s \\ & o r \\ & W=(F \cos \theta) d \\ & \hline \end{aligned}$ | 6.1 |
| :---: | :---: | :---: |
| Kinetic Energy | $K E=\frac{1}{2} m v^{2}$ | 6.2 |
| Work-Energy Theorem | $\begin{aligned} W= & K E_{f}-K E_{0} \\ & =\frac{1}{2} m v_{f}^{2}-\frac{1}{2} m v_{0}^{2} \\ & =\frac{1}{2} m\left(v_{f}^{2}-v_{0}^{2}\right) \end{aligned}$ | 6.3 |
| Work done by gravity | $W_{\text {gravity }}=m g\left(h_{0}-h_{f}\right)$ | 6.4 |
| Gravitational Potential Energy | $P E=m g h$ | 6.5 |
| Alternative Work-Energy Theorem | $\begin{gathered} W_{n c}=E_{f}-E_{0} \\ =\left(K E_{f}+P E_{f}\right)-\left(K E_{0}+P E_{0}\right) \end{gathered}$ | 6.8 |
| When $W_{n c}=0$ | $\begin{gathered} E_{f}=E_{0} \text { or } \\ \left(K E_{f}+P E_{f}\right)=\left(K E_{0}+P E_{0}\right) \end{gathered}$ |  |
| Power | $P=\frac{W}{t}=\frac{\Delta E}{t}=F v$ | $\begin{aligned} & 6.10 \\ & 6.11 \end{aligned}$ |
| Work done by a variable Force | Area under the curve of a $F \cos \theta$ vs. s graph |  |

- Conservative Forces: force of gravity, spring force
- Non-conservative forces: friction, air resistance

Chapter 7

| Impulse and Momentum |  |  |
| :--- | :---: | :--- |
| Impulse | $J=\bar{F} \Delta t$ | 7.1 |
| Linear Momentum, p | $p=m v$ | 7.2 |
| $\begin{array}{l}\text { Impulse-Momentum } \\ \text { Theorem }\end{array}$ | $\left(\sum \bar{F}\right) \Delta t=m v_{f}-m v_{0}=m \Delta v$ |  |
| Or $\mathrm{J}=\Delta \mathrm{p}$ |  |  |$] 7.4$

## Collision

| Final Velocity of 2 <br> objects in a head-on <br> collision where one <br> object is initially at rest <br> 1: moving object <br> 2: object at rest | $v_{f 1}=\left(\frac{m_{1}-m_{2}}{m_{1}+m_{2}}\right) v_{01}$ |  |
| :--- | :---: | :--- |
| Conservation of Linear <br> Momentum (in 1D) | $v_{f 2}=\left(\frac{2 m_{1}}{m_{1}+m_{2}}\right) v_{01}$ | 7.8 |
| Elastic Collision | $\vec{P}_{0}=\vec{P}_{f}=\vec{P}_{f}-\vec{P}_{0}=0$ | 7.7 |
| Inelastic Collision | $m_{1} v_{01}+m_{2} v_{02}=m_{1} v_{f 1}+m_{2} v_{f 2}$ | 7.7 b |
| Conservation of Linear <br> Momentum (in 2D) | $m_{1} v_{01}+m_{2} v_{02}=\left(m_{1}+m_{2}\right) v_{f}$ <br> $m_{1} v_{01 x}+m_{2} v_{02 x}=m_{1} v_{f 1 x}+m_{2} v_{f 2 x}$ <br> $m_{1} v_{02 y}=m_{1} v_{f 1 y}+m_{2} v_{f 2 y}$ | 7.9 |

Center of Mass

| Center of mass <br> location | $x_{c m}=\frac{m_{1} x_{1}+m_{2} x_{2}}{m_{1}+m_{2}}$ | 7.10 |
| :--- | :---: | :---: |
| Center of mass velocity | $v_{c m}=\frac{m_{1} v_{1}+m_{2} v_{2}}{m_{1}+m_{2}}$ | 7.11 |

## Chapter 8

| Angular displacement | $\Delta \theta=\theta-\theta_{0}$ <br> $\theta=\frac{s}{r}$ | 8.1 |
| :--- | :---: | :--- |
| Average angular <br> velocity | $\bar{\omega}=\frac{\Delta \theta}{\Delta t}$ | 8.2 |
| Average angular <br> acceleration | $\bar{\alpha}=\frac{\Delta \omega}{\Delta t}$ | 8.4 |

## Motion of a particle with constant acceleration

| $\omega=\omega_{0}+\alpha t$ | 8.4 |
| :---: | :---: |
| $\theta=\frac{1}{2}\left(\omega+\omega_{0}\right) t$ | 8.6 |
| $\theta=\omega_{0} t+\frac{1}{2} \alpha t^{2}$ | 8.7 |
| $\omega^{2}=\omega_{0}^{2}+2 \alpha \theta$ | 8.8 |


| Relationship between |  |  |
| :--- | :---: | :---: |
| angular variables and | $v_{T}=r \omega$ |  |
| tangential variables (t |  |  |
| subscript) | $a_{T}=r \alpha$ | 8.9 |
|  |  | 8.10 |
| When no slipping | $v=v_{T}=r \omega$ <br> $a=a_{T}=r \alpha$ | 8.12 |
| Centripetal acceleration | $a_{c}=r \omega^{2}$ | 8.13 |

Chapter 9

| Torque and Inertia |  | 9.1 |
| :--- | :---: | :---: |
| When at Equilibrium $\tau$ | $\tau=F \ell$ | 9.2 |
| Moment of Inertia | $I=\sum m r^{2}$ | 9.6 |
| Newton's Second Law <br> for a rigid body <br> rotating about a Fixed <br> axis | $\sum \tau=I \alpha$ | 9.7 |

Work, Energy

| Rotational work | $W_{R}=\tau \theta$ | 9.8 |
| :--- | :---: | :---: |
| Rotational Kinetic <br> Energy | $K E_{R}=\frac{1}{2} I \omega^{2}$ | 9.9 |


| Angular Momentum | $L=I \omega$ | 9.1 |
| :--- | :---: | :--- |
| Center of Gravity | $x_{c g}=\frac{W_{1} x_{1}+W_{1} x_{1}+\cdots}{W_{1}+W_{2}+\cdots}$ | 9.2 |

See reverse side for moments of Inertia I for various rigid objects of Mass M

## Moments of Inertia I for various rigid objects of Mass $M$

| Thin walled hollow cylinder or hoop $I=M R^{2}$ | Solid cylinder or disk |
| :---: | :---: |
| Thin rod, axis perpendicular to rod and passing though center $I=\frac{1}{12} M L^{2}$ | Thin rod, axis perpendicular to rod and passing though end $I=\frac{1}{3} M L^{2}$ |
| Solid Sphere, axis through center | Solid Sphere, axis tangent to surface $I=\frac{7}{5} M R^{2}$ |
| Thin Walled spherical shell, axis through center $I=\frac{2}{3} M R^{2}$ | Thin Rectangular sheet, axis along one edge $I=\frac{1}{3} M L^{2}$ |
| Thin Rectangu | sheet, axis parallel to sheet and passing gh center of the other edge $I=\frac{1}{12} M L^{2}$ |

## Chapter 10

| Force Applied | $F_{x}^{\text {applied }}=k x$ | 10.1 |
| :--- | :---: | :--- |
| Hooke's Law | $F_{x}=-k x$ | 10.2 |
| Frequency <br> cycles per time | $f=\frac{1}{T}$ | 10.5 |
| Angular frequency | $\omega=2 \pi f=2 \pi / T$ | 10.6 |
| Maximum Velocity <br> Simple Harmonic <br> Motion | $v_{\max }=A \omega$ | 10.8 |
| Maximum Acceleration <br> Simple Harmonic <br> Motion | $a_{\max }=A \omega^{2}$ | 10.11 |
| Angular frequency of <br> simple harmonic <br> motion | $\quad P=\sqrt{k / m}$ | 10.11 |
| Elastic potential <br> energy | PE elastic $=\frac{1}{2} k x^{2}$ | 10.13 |

## Simple Pendulum (10.16)

| Angular Frequency | Time Period | Length |
| :---: | :---: | :---: |
| $\omega=\sqrt{\frac{g}{L}}$ | $T=2 \pi \sqrt{\frac{L}{g}}$ | $L=\frac{T^{2} g}{4 \pi^{2}}$ |

Physical pendulum (10.15)

| Angular Frequency | Time Period |
| :---: | :---: |
| $\omega=\sqrt{\frac{m g L}{I}}$ | $T=2 \pi \sqrt{\frac{I}{m g L}}$ |

Elastic deformation -stretch and compression (10.17)
Perpendicular to Area (A)
$Y=$ constant called Young's modulus

| Force | Change in Length |
| :---: | :---: |
| $F=Y\left(\frac{\Delta L}{L_{0}}\right) A$ | $\Delta L=\frac{F L_{0}}{Y A}$ |

## Shear Deformation (change in shape)

Parallel to Area (A)
$S$ = constant called the shear modulus

| Force |  |
| :---: | :---: |
| $F=S\left(\frac{\Delta X}{L_{0}}\right) A$ | Change in Length |
|  | $\Delta \mathrm{X}=\frac{F L_{0}}{S A}$ |

## Pressure (related to Volume deformation)

$$
P=\frac{F}{A}
$$

change $\Delta P$ in pressure needed to change the volume
$B=$ constant known as the bulk modulus When the volume decreases, $\Delta V$ is negative

$$
\Delta P=-B\left(\frac{\Delta V}{V_{o}}\right)
$$

Chapter 11

| Density | $\rho=\frac{m}{V}$ | 11.1 |
| :---: | :---: | :---: |
| Pressure | $P=\frac{F}{A}$ | 11.3 |
| Specific Gravity | $=\frac{\text { Density of substance }}{1.000 \times 10^{3} \mathrm{~kg} / \mathrm{m}^{3}}$ | 11.2 |
| Pressure and depth in a static Fluid $P_{1}$ is higher than $P_{2}$ | $P_{2}=P_{1}+\rho g h$ | 10.4 |
| Gauge Pressure | $\rho g h$ |  |
| Archimedes’ principle | $F_{B}=W_{\text {fluid }}$ | 11.6 |
| Mass Flow Rate | Mass flow rate $=\rho A v$ | 11.7 |
| Volume flow rate | $Q=A v=\frac{V}{t}$ |  |
| Bernoulli's Equation | $P_{1}+\frac{1}{2} \rho v_{1}^{2}+\rho g y_{1}=P_{2}+\frac{1}{2} \rho v_{2}^{2}+\rho g y_{2}$ | 11.11 |
| Equation of continuity | $\rho_{1} A_{1} v_{1}=\rho_{2} A_{2} v_{2}$ | 11.8 |
| equation of continuity ( $\rho_{1}=\rho_{2}$ ) | $A_{1} v_{1}=A_{2} v_{2}$ |  |
| Force to move Viscous Layer with constant velocity | $F=\frac{\eta A v}{y}$ | 11.13 |
| Poiseuille's law | $Q=\frac{\pi R^{4}\left(P_{2}-P_{1}\right)}{8 \eta L}$ | 11.14 |
| Force and Area if Pressure same | $F_{1} / A_{1}=F_{2} / A_{2} \text { or } F_{2}=F_{1}\left(\frac{A_{2}}{A_{1}}\right)$ |  |

## Chapter 12

Temperature Scales

| Fahrenheit to <br> Celsius | Temperature |  |  |
| :--- | :---: | :---: | :---: |
| Celsius to <br> Fahrenheit |  | $F=\frac{5}{5} C+32$ |  |
| Celsius to Kelvin |  | $\mathrm{K}=\mathrm{C}+273.15$ or $T=$ <br> $T_{c}+273.15$ | 12.1 |

Thermal Expansion

| Linear Thermal <br> Expansion | $\Delta L=\alpha L_{o} \Delta T$ | 12.2 |
| :--- | :---: | :---: |
| Volume Thermal <br> Expansion | $\Delta V=\beta V_{0} \Delta T$ | 12.3 |


| Heat and Power |  |  |
| :--- | :---: | :---: |
| Heat and temperature <br> change | $\Delta Q=c m \Delta T$ | 12.4 |
| Heat and phase change | $Q=m L$ | 12.5 |


| \% Relative Humidity | $\frac{\text { Partial } P_{\text {water vapot }}}{\text { Equilibrum } P_{\text {water vapot }} @ \text { temp }}$ | 12.6 |
| :--- | :---: | :---: |

Chapter 13

| Heat and Power |
| :--- |
| Power $\mathrm{P}=\mathrm{Q} / \mathrm{t}$  <br> Heat Conducted $Q=\frac{(k A \Delta T) t}{L}$ 13.1 <br> Radiant energy <br> e emissivity <br> $\sigma=5.67 \times 10^{-8} \mathrm{~J} /\left(\mathrm{s}^{*} \mathrm{~m}^{2} *^{4}\right)$ $Q=e \sigma T^{4} A t$  <br> T temp in Kelvins <br> A surface area $P_{n e t}=e \sigma A\left(T^{4}-T_{0}^{4}\right)$ 13.3 <br> Net radiant Power <br> T object Temp in kelvins <br> To environment temp in <br> Kelvins   |

Table 13.1 Thermal Conductivities ${ }^{a}$ of Selected Materials
Substance Thermal Conductivity, $k\left[\mathrm{~J} /\left(\mathrm{s} \cdot \mathrm{m} \cdot \mathrm{C}^{\circ}\right)\right]$

## Metals

| Aluminum | 240 |
| :--- | :--- |
| Brass | 110 |
| Copper | 390 |
| Iron | 79 |
| Lead | 35 |
| Silver | 420 |
| Steel (stainless) | 14 |

Gases

| Air | 0.0256 |
| :--- | :--- |
| Hydrogen $\left(\mathrm{H}_{2}\right)$ | 0.180 |
| Nitrogen $\left(\mathrm{N}_{2}\right)$ | 0.0258 |
| Oxygen $\left(\mathrm{O}_{2}\right)$ | 0.0265 |

## Other Materials

| Asbestos | 0.090 |
| :--- | :--- |
| Body fat | 0.20 |
| Concrete | 1.1 |
| Diamond | 2450 |
| Glass | 0.80 |
| Goose down | 0.025 |
| Ice ( $\left.0^{\circ}{ }^{\circ} \mathrm{C}\right)$ | 2.2 |
| Styrofoam | 0.010 |
| Water | 0.60 |
| Wood (oak) | 0.15 |
| Wool | 0.040 |
| Except as noted, the valves pertain to temperatures near $20{ }^{\circ} \mathrm{C}$. |  |

## Chapter 14

Molecular Mass, Moles, and Avogadro's Number

| Atomic Mass Unit | $1 u=1.6605 \times 10^{-27} \mathrm{~kg}$ |
| :--- | :---: |
| Avogadro's Number | $N_{A}=6.022 \times 10^{23} \mathrm{~mol}^{-1}$ |
| Number of Moles, n <br> N number of particles (atoms or <br> molecules) | $n=\frac{\mathrm{N}}{N_{A}}$ |
| Number of Moles, n <br> m sample mass (g) <br> mass per mole: g/mol | $m_{\text {particle }}=\frac{\mathrm{mass} \text { per mole }}{N_{A}}$ |
| Mass of a particle | $\rho=\frac{n \cdot \text { mass per mole }}{\mathrm{man}}$ |
| Density |  |

## Ideal Gas Law

| Ideal Gas law |  |  |
| :--- | :---: | :---: |
| n number of moles |  |  |
| R Universal gas constant $=8.31 \mathrm{~J} /(\mathrm{mol} * \mathrm{~K})$ | $P V=n R T$ | 14.1 |
| T temp kelvins |  |  |
| Ideal Gas Law (alternative form) <br> N number of particles <br> k Boltzmann's constant $\left(1.38 \times 10^{-23} \mathrm{~J} \mathrm{~K}^{-1}\right)$ | $P V=N k T$ | 14.2 |

## Boyle's and Charles' Laws

| Boyle's law <br> (when n and T are <br> constant) | $P_{i} V_{i}=P_{f} V_{f}$ | 14.3 |
| :--- | :---: | :---: |
| Charles' law <br> (n and P are constant) | $\frac{V_{i}}{T_{i}}=\frac{V_{f}}{T_{f}}$ | 14.4 |

## Energy

| Average Kinetic Energy <br> for a molecule | $\overline{K E}=\frac{1}{2} m v_{r m s}^{2}=\frac{3}{2} k T$ | 14.6 |
| :--- | :---: | :---: |
| Internal Energy | $U=\frac{3}{2} n R T$ | 14.7 |

Diffusion

| Fick's law of diffusion |  |  |
| :--- | :--- | :--- |
| D Diffusion constant |  |  |
| $\Delta C$ is the solute | $m=\frac{D A \Delta C t}{L}$ | 14.8 |
| concentration |  |  |
| difference between the |  |  |
| ends of the channel |  |  |
| (same as density) |  |  |

## Chapter 15

First Law of Thermodynamics

| First Law | $\Delta U=U_{f}-U_{0}=Q-W$ | 15.1 |
| :--- | :--- | :--- |
| Note: |  |  |
| $\Delta U$ Change in Internal Energy |  |  |
| Q (heat) is positive when the system gains heat and negative when it loses |  |  |
| heat. W (work) is positive when work is done by the system and negative |  |  |
| when work is done on the system. |  |  |


| Applications of First Law |  |  |
| :--- | :---: | :---: |
| Process | Work Done | First Law |
| Isobaric <br> (constant pressure) | $W=P\left(V_{f}-V_{i}\right)$ <br> (Eq 15.2) | $\Delta U=Q-P\left(V_{f}-V_{i}\right)$ <br> $\left(Q=\frac{5}{2} n R \Delta T\right)$ |
| Isochoric <br> (constant volume) | $\mathrm{W}=0 \mathrm{~J}$ | $\Delta U=Q-0 J$ <br> $\left(Q=\frac{3}{2} n R \Delta T\right)$ |
| Isothermal <br> (constant temp) | $W=n R T \ln \left(\frac{V_{f}}{V_{i}}\right)$ <br> (Eq. 15.3) | $O J=Q-n R T \ln \left(\frac{V_{f}}{V_{i}}\right)$ |
| Adiabatic <br> (no heat flow) | $W=\frac{3}{2} n R\left(T_{i}-T_{f}\right)$ <br> $(15.4)$ | $\Delta U=0 J-\frac{3}{2} n R\left(T_{i}-T_{f}\right)$ |


| Adiabatic <br> expansion/compression <br> of an ideal gas | $P_{0} V_{0}^{\gamma}=P_{f} V_{f}^{\gamma}$ | 15.5 |
| :--- | :---: | :---: |
| Heat with known <br> number of moles | $Q=C n \Delta T$ | 15.6 |
| molar specific heat | $C_{p}=\frac{5}{2} R$ | 15.7 |
|  | $C_{v}=\frac{3}{2} R$ | 15.8 |

Heat Engines

| The efficiency e of a <br> heat engine | $e=\frac{\text { Work done }}{\text { Input heat }}=\frac{\|W\|}{\left\|Q_{H}\right\|}=1-\frac{\left\|Q_{c}\right\|}{\left\|Q_{H}\right\|}$ | 15.11 <br> 15.13 |
| :--- | :---: | :---: |
| Conservation of energy <br> requires | $\left\|Q_{H}\right\|=\|W\|+\left\|Q_{c}\right\|$ | 15.12 |

Carnot Engine

| Carnot Engine |  |  |
| :--- | :---: | :---: |
| For a Carnot engine | $\frac{\left\|Q_{C}\right\|}{\left\|Q_{H}\right\|}=\frac{\left\|T_{C}\right\|}{\left\|T_{H}\right\|}$ | 14.14 |
| Efficiency e for a <br> Carnot engine | $e_{\text {carnot }}=1-\frac{T_{C}}{T_{H}}$ | 15.15 |

Coefficient of Performance (COP)

| COP of a refrigerator or <br> an air conditioner | $C O P=\frac{\left\|Q_{c}\right\|}{\|W\|}=\frac{1}{\frac{T_{H}}{T_{C}}-1}$ |  |
| :--- | :---: | :---: |
| COP of a heat pump | $C O P=\frac{\left\|Q_{H}\right\|}{\|W\|}$ | 15.17 |

Entropy

| change in entropy $\Delta S$ | $\Delta S=\left(\frac{Q}{T}\right)_{R}$ | 15.18 |
| :---: | :---: | :---: |
| change in entropy <br> $\Delta \boldsymbol{S}_{\text {universal }}$ | $\begin{aligned} \Delta S_{\text {universal }} & =\Delta S_{\text {system }}+\Delta S_{\text {surroundings }} \\ & =\Delta S_{\text {cold }}+\Delta S_{\text {Hot }} \end{aligned}$ |  |
| Energy unavailable for doing work | $W_{\text {unavailable }}=T_{0} \Delta S_{\text {universe }}$ | 15.19 |

## Chapter 16

| Waves |  |  |
| :--- | :---: | :---: |
| Speed of a Wavelength | $v=f \lambda=\frac{\lambda}{T}$ | 16.1 |
| Speed of a wave on a <br> string | $v=\sqrt{\frac{F}{m / L}}$ | 16.2 |
| description <br> $+x$ direction | $y=A \sin \left(2 \pi f t-\frac{2 \pi x}{\lambda}\right)$ | 16.3 |
| description <br> $-x$ direction | $y=A \sin \left(2 \pi f t+\frac{2 \pi x}{\lambda}\right)$ | 16.4 |

Speed of Sound

| Speed of Sound in a <br> Gas <br> $\mathrm{k}=1.38 \times 10^{-23}$ | $v=\sqrt{\frac{\gamma k T}{m}}$ | 16.5 |
| :--- | :---: | :---: |
| Speed of sound in a <br> liquid | $v=\sqrt{\frac{B_{a d}}{\rho}}$ | 16.6 |
| Speed of sound in solid <br> bar | $v=\sqrt{\frac{Y}{\rho}}$ | 16.7 |

Sound Intensity

| Sound Intensity |  |  |
| :--- | :---: | :--- |
| Intensity | $I=\frac{P}{A}$ | 16.8 |
| Intensity -uniform in <br> all directions | $I=\frac{P}{4 \pi r^{2}}$ | 16.9 |
| Intensity level in <br> decibels <br> $10=1 \times 10-12 \mathrm{~W} / \mathrm{m} 2$ | $\beta=(10 d B) \log \left(\frac{I}{I_{o}}\right)$ | 16.10 |


| Doppler Effect |  |  |
| :--- | :---: | :---: |
| Source Moving toward <br> stationary observer | $f_{o}=f_{S}\left(\frac{1}{1-\frac{v_{S}}{v}}\right)$ | 16.15 |
| Source Moving away <br> from stationary <br> observer | $f_{o}=f_{S}\left(\frac{1}{1+\frac{v_{S}}{v}}\right)$ | 16.15 |
| Observer moving <br> toward stationary <br> source | $f_{o}=f_{s}\left(1+\frac{v_{o}}{v}\right)$ | 16.15 |
| Observer moving away <br> from stationary source | $f_{o}=f_{s}\left(1-\frac{v_{o}}{v}\right)$ | 16.15 |

## Chapter 17

Constructive and Destructive Interference

| Constructive | Difference in path lengths is zero or an integer |
| :--- | :--- |
| 2 waves in Phase | $(0,1,2,3 \ldots)$ |
| Destructive | Difference in path lengths is a half- integer |
| 2 waves in Phase | $(0.5,1.5,2.5, \ldots)$ |
| Constructive | Difference in path lengths is a half- integer |
| 2 waves out of Phase | $(0.5,1.5,2.5, \ldots)$ |
| Destructive | Difference in path lengths is zero or an integer |
| 2 waves out of Phase | $(0,1,2,3 \ldots)$ |

Diffraction

| Single Slit -first minimum | $\sin \theta=\frac{\lambda}{D}$ | 17.1 |
| :--- | :---: | :--- |
| Circular Opening -first minimum | $\sin \theta=1.22 \frac{\lambda}{D}$ | 17.2 |


| beats | $f_{\text {beat }}=f_{1}-f_{2}$ | 17.46 |
| :--- | :--- | :--- |


| Standing Waves |  |  |
| :--- | :---: | :---: |
| Transverse <br> Natural frequency <br> Fixed at both ends | $f_{n}=n\left(\frac{v}{2 L}\right)$ for $\mathrm{n}=1,2, \ldots$ | 17.3 |
| Longitudinal <br> Natural frequency <br> open at both ends | $f_{n}=n\left(\frac{v}{2 L}\right)$ for $\mathrm{n}=1,2, \ldots$ | 17.4 |
| Longitudinal <br> Natural frequency <br> open at one end | $f_{n}=n\left(\frac{v}{4 L}\right)$ for $\mathrm{n}=1,3,5, \ldots$ | 17.5 |

## Chapter 18

Formulas

| Number of <br> electrons/protons | $\#=\frac{q}{e}$ |  |
| :--- | :---: | :--- |
| Coulombs law: <br> F=force <br> Where one exerts on <br> two | $F=\frac{k\left\|q_{1}\right\|\left\|q_{2}\right\|}{r^{2}}$ | 18.1 |
| Electric Field | $\vec{E}=\frac{\vec{F}}{q_{0}}$ | 18.2 |
| Magnitude of Electric <br> Field | $E=\frac{k\|q\|}{r^{2}}$ | 18.3 |
| Magnitude of Electric <br> Field for a parallel <br> plate capacitor | $\Phi_{E}=\sum(E \cos \phi) \Delta A=\frac{q}{\epsilon_{0} A}=\frac{\sigma}{\epsilon_{0}}$ | $18.6,7$ |
| Electric Flux |  | 18.4 |

## Important Numbers

| $k=8.99 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}$ |
| :---: |
| Permittivity of free space |
| $\epsilon_{0}=8.85 \times 10^{-12} \frac{\mathrm{C}^{2}}{\mathrm{~N} \cdot \mathrm{~m}^{2}}$ |
| Magnitude of charge on electron (-e) or proton (+e) |
| $e=1.6 \times 10^{-19} \mathrm{C}$ (a lot of time $q_{0}$ ) |
| Mass of Electron |
| $9.11 \times 10^{-31} \mathrm{~kg}$ |
| Mass of Proton |
| $1.673 \times 10^{-27} \mathrm{~kg}$ |
| Mass of Neutron |
| $1.675 \times 10^{-27} \mathrm{~kg}$ |

Chapter 19

## Chapter 20

| Work and Electric Potential Energy | $W_{A B}=E P E_{A}-E P E_{B}$ | 19.1 |
| :---: | :---: | :---: |
| Electric Potential | $V=\frac{E P E}{q_{0}}=\frac{k q}{r}$ | 19.3,6 |
| Electric Potential Difference Charge moves from A to B | $V_{A}-V_{B}=\frac{E P E_{B}}{q_{0}}-\frac{E P E_{A}}{q_{0}}=\frac{-W_{A B}}{q_{0}}$ | 19.4 |
| Electric Potential Difference Charge moves from B to A | $V_{B}-V_{A}=\frac{W_{A B}}{q_{0}}$ |  |
| Total Energy | $\begin{gathered} E=\frac{1}{2} m v^{2}+\frac{1}{2} I \omega^{2}+m g h+\frac{1}{2} k x^{2} \\ +E P E \end{gathered}$ |  |
| Electric field | $E=-\frac{\Delta V}{\Delta s}$ | 19.7a |
| Charge on each plate of a capacitor | $q=C V$ |  |
| Dielectric constant (E's are electric fields without and with a dielectric) | $\kappa=\frac{E_{o}}{E}$ |  |
| Capacitance of a parallel plate capacitor | $C=\frac{\kappa \epsilon_{0} A}{d}$ |  |
| Electric Potential Energy Stored in a capacitor | Energy $=\frac{1}{2} q V=\frac{1}{2} C V^{2}=\frac{q^{2}}{2 C}$ | 19.11 |
| Energy Density | Energy Density $=\frac{\text { Energy }}{\text { Volume }}=\frac{1}{2} \kappa \epsilon_{0} E^{2}$ | 19.12 |


| Current (if electric current is constant) | $I=\frac{\Delta q}{\Delta t}$ | 20.1 |
| :---: | :---: | :---: |
| Ohms Law | $V=I R$ or $R=\frac{V}{I}$ or $I=\frac{V}{R}$ | 20.2 |
| Resistance with length L, cross-sectional area A | $R=\rho \frac{L}{A}$ | 20.3 |
| Resistance and Resistivity (T temp) | $\begin{aligned} & \rho=\rho_{0}\left[1+\alpha\left(T-T_{0}\right)\right] \\ & R=R_{0}\left[1+\alpha\left(T-T_{0}\right)\right] \end{aligned}$ | 20.4,5 |
| Electric Power | $P=I V, \quad P=I^{2} R, \quad P=\frac{V^{2}}{R}$ | 20.6 |
| AC Circuits | $\begin{aligned} V & =V_{0} \sin (2 \pi f t) \\ I & =I_{0} \sin (2 \pi f t) \end{aligned}$ | 20.7,8 |
| RMS Formulas with Current and Voltage | $\begin{aligned} & I_{r m s}=\frac{I_{0}}{\sqrt{2}} \\ & V_{r m s}=\frac{V_{0}}{\sqrt{2}} \end{aligned}$ | $\begin{aligned} & 20.12 \\ & 20.13 \end{aligned}$ |
| Average Power | $\begin{gathered} \bar{P}=I_{r m s} V_{r m s} \\ \bar{P}=I_{r m s}^{2} R \\ \bar{P}=\frac{V_{r m s}^{2}}{R} \end{gathered}$ | 20.15 |
| Series <br> (I is the same) | $\begin{aligned} & R_{S}=R_{1}+R_{2}+R_{3}+\cdots \\ & \frac{1}{C_{S}}=\frac{1}{C_{1}}+\frac{1}{C_{2}}+\frac{1}{C_{3}}+\cdots \end{aligned}$ | $\begin{aligned} & 20.16 \\ & 20.19 \end{aligned}$ |
| Parallel <br> ( V is the same) | $\begin{aligned} & \frac{1}{R_{s}}=\frac{1}{R_{1}}+\frac{1}{R_{2}}+\frac{1}{R_{3}}+\cdots \\ & C_{p}=C_{1}+C_{2}+C_{3}+\cdots \end{aligned}$ | $\begin{aligned} & 20.17 \\ & 20.18 \end{aligned}$ |
| RC circuits | $\begin{gathered} q=q_{0}\left[1-e^{\left.\frac{-t}{R C}\right]}\right. \text { (charging) } \\ \tau=R C \\ q=q_{0} e^{\frac{-t}{R C}} \text { (discharging) } \end{gathered}$ | $\begin{aligned} & 20.20 \\ & 20.21 \\ & 20.22 \end{aligned}$ |

Chapter 22

| Magnitude of magnetic Field $\mu_{0}=4 \pi \times 10^{-7} T \cdot m / A$ | $\begin{gathered} B=\frac{F}{\left\|q_{0}\right\| v \sin \theta} \\ B=\frac{\mu_{0} I}{2 \pi r} \\ B=N \frac{\mu_{0} I}{2 R} \\ B=\mu_{0} n I \end{gathered}$ | $\begin{aligned} & 21.1 \\ & 21.5 \\ & 21.6 \\ & 21.7 \end{aligned}$ |
| :---: | :---: | :---: |
| Radius of circular path of particle caused by F | $r=\frac{m v}{\|q\| B}$ | 21.2 |
| Relationship between Mass and B | $m=\left(\frac{e r^{2}}{2 V}\right)^{2} B^{2}$ |  |
| Force on a current in a magnetic field | $F=I L B \sin \theta$ | 21.3 |
| Torque on a currentcarrying coil | $\tau=N I A B \sin \phi$ <br> $\phi$ is the angle between direction of $B$ and the normal plane | 21.4 |
| Ampere's Law | $\sum B_{\\|} \Delta l=\mu_{0} I$ | 21.8 |

RHR 1: Fingers point along the direction of $\vec{B}$ and the thumb points along the velocity $\vec{v}$ The palm of the hand then faces in the direction of $\vec{F}$ that acts on a positive charge.

RHR 2: Curl the fingers of the right hand into a half-circle. Point the thumb in the direction of the conventional current I, and the tips of the fingers will point in the direction of $\vec{B}$

| Motional emf | $\mathcal{E}=v B L$ | 22.1 |
| :---: | :---: | :---: |
| Magnetic Flux | $\Phi=B A \cos \phi$ | 22.2 |
| Faraday's Law | $\mathcal{E}=-N \frac{\Delta \Phi}{\Delta t}$ | 22.3 |
| Emf induced ion a rotating planar coil $\omega=2 \pi f$ | $\mathcal{E}=N A B \omega \sin (\omega t)=\mathcal{E}_{0} \sin (\omega t)$ | 22.4 |
| Current | $I=\frac{V-\mathcal{E}}{R}$ | 22.5 |
| Mutual Inductance | $M=\frac{N_{s} \Phi_{s}}{I_{p}}$ | 22.6 |
| Emf due to mutual inductance | $\mathcal{E}_{s}=-M \frac{\Delta I_{p}}{\Delta t}$ | 22.7 |
| Self-Inductance | $L=\frac{N \Phi}{I}$ | 22.8 |
| Emf due to selfinductance | $\mathcal{E}_{s}=-L \frac{\Delta I}{\Delta t}$ | 22.9 |
| Energy stored in an inductor | Energy $=\frac{1}{2} L I^{2}$ | 22.10 |
| Energy Density | Energy Density $=\frac{1}{2 \mu_{0}} B^{2}$ | 22.11 |
| Voltage and turns of primary and secondary coil | $\frac{V_{s}}{V_{p}}=\frac{N_{s}}{N_{p}}$ | 22.12 |
| Current and turns of primary and secondary coil | $\frac{I_{s}}{I_{p}}=\frac{N_{p}}{N_{s}}$ | 22.13 |
| Power | Power=Energy*time |  |

Chapter 23
Chapter 24

| Rms Voltage across a <br> capacitor | $V_{r m s}=I_{r m s} X_{C}$ | 23.1 |
| :--- | :---: | :--- |
| Capacitive Reactance | $X_{C}=\frac{1}{2 \pi f C}$ | 23.2 |
| Rms Voltage across an <br> inductor | $V_{r m s}=I_{r m s} X_{L}$ | 23.3 |
| Inductive Reactance | $X_{L}=2 \pi f L$ | 23.4 |
| Rms Voltage for <br> circuit containing <br> resistance capacitance, <br> and inductance | $V_{r m s}=I_{r m s} Z$ | 23.6 |
| Impedance of a <br> resistor, capacitor and <br> inductor connected in a <br> series | $Z=\sqrt{R^{2}+\left(X_{L}-X_{C}\right)^{2}}$ | 23.7 |
| Tangent of the phase <br> angle | $\bar{P}=I_{r m s} V_{r m s} \cos \phi$ | 23.8 |
| Average Power | $f_{0}=\frac{1}{2 \pi \sqrt{L C}}$ | 23.9 |
| Resonant frequency | power factor $=\frac{X_{L}-X_{C}}{Z}$ | 23.10 |
| Power Factor |  |  |


| Speed of Light | $c=3.00 \times 10^{8} \mathrm{~m} / \mathrm{s}$ |  |
| :--- | :---: | :--- |
| Speed of Light in a <br> vacuum | $c=\frac{1}{\sqrt{\varepsilon_{0} \mu_{0}}}$ | 24.1 |
| Total energy density | $u=\frac{1}{2} \varepsilon_{0} E^{2}+\frac{1}{2 \mu_{0}} B^{2}$ <br> $u=\varepsilon_{0} E^{2}$ <br> $u=\frac{1}{\mu_{0}} B^{2}$ | 24.2 |
| Relationship between <br> magnitudes Electric <br> and magnetic field <br> waves | $E=c B$ | 2.43 |
| Rms for Electric Field | $E_{r m s}=\frac{1}{\sqrt{2}} E_{0}$ | 24.4 |
| Rms for Magnetic <br> Field | $B_{r m s}=\frac{1}{\sqrt{2}} B_{0}$ | $24=c U$ |

## Chapter 25

Concave Mirror

| Focal length Concave <br> mirror | $f=\frac{1}{2} R$ | 25.1 |
| :--- | :--- | :--- |
| Focal length Convex <br> Mirror | $f=-\frac{1}{2} R$ | 25.2 |
| Mirror Equation | $\frac{1}{d_{o}}+\frac{1}{d_{i}}=\frac{1}{f}$ | 25.3 |
| Magnification <br> Equation | $m=-\frac{d_{i}}{d_{o}}$ <br> $m=\frac{h_{i}}{h_{o}}$ | 25.4 |

## Plain Mirror

- Forms an upright virtual image
- Image located same distance behind the mirror as the object in front
- Heights of object and virtual image the same

Information for Spherical mirrors

| Focal Length | + | Concave mirror |
| :--- | :--- | :--- |
|  | - | Convex mirror |
| Object distance | + | Object in front (real) |
|  | - | Object behind (virtual) |
| Image Distance | + | Image in front (real) |
|  | - | Image behind (virtual) |
| Magnification (sign) | + | Image is upright |
|  | - | Image is inverted |
| Magnification <br> (magnitude) | $>1$ | larger |
|  | $<1$ | smaller |

